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► **To cite this version:**

Utku Acer, Paolo Giaccone, David Hay, Giovanni Neglia, Saed Tarapiah. Timely Data Delivery in a Realistic Bus Network. [Research Report] RR-7344, INRIA. 2010. inria-00547254

**HAL Id: inria-00547254**

**<https://hal.inria.fr/inria-00547254>**

Submitted on 15 Dec 2010

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# *Timely Data Delivery in a Realistic Bus Network*

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N° 7344

August 2010

—— Networks and Telecommunications ——



*rapport  
de recherche*



## Timely Data Delivery in a Realistic Bus Network

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Theme : Networks and Telecommunications  
Networks, Systems and Services, Distributed Computing  
Équipe-Projet Maestro

Rapport de recherche n° 7344 — August 2010 — 32 pages

**Abstract:** WiFi-enabled buses and stops may form the backbone of a metropolitan delay tolerant network, that exploits nearby communications, temporary storage at stops, and predictable bus mobility to deliver non-real time information.

This paper studies the problem of how to route data from its source to its destination in order to maximize the delivery probability by a given deadline. We assume to know the bus schedule, but we take into account that randomness, due to road traffic conditions or passengers boarding and alighting, affects bus mobility. In this sense, this paper is one of the first to tackle *quasi-deterministic* mobility scenarios.

We propose a simple stochastic model for bus arrivals at stops, supported by a study of real-life traces collected in a large urban network with 250 bus lines and about 7500 bus-stops. A succinct graph representation of this model allows us to devise an optimal (under our model) single-copy routing algorithm and then extend it to cases where several copies of the same data are permitted.

Through an extensive simulation study, we compare the optimal routing algorithm with three other approaches: minimizing the expected traversal time over our graph, maximizing the delivery probability over an infinite time-horizon, and a recently-proposed heuristic based on bus frequencies. We show that, in general, our optimal algorithm outperforms the three, but it essentially reduces to either minimizing the expected traversal time when transmissions are always successful, or maximizing the delivery probability over an infinite time-horizon when transmissions fail frequently. For reliable transmissions and “reasonable” values of deadlines, the multi-copy extension requires only 10 copies to reach almost the performance of costly flooding approaches.

**Key-words:** Delay Tolerant Networks, Quality of Service, Optimal Routing

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## **Livraison des données dans les délais pour un réseau d'autobus réaliste**

**Résumé :** Bus et arrêts avec capacités de transmission WiFi peuvent constituer l'épine dorsale d'un réseau urbain tolérant aux délais, qui exploite les transmissions à courte portée, le stockage temporaire des données aux arrêts, et la mobilité prévisible de bus pour délivrer des informations non en temps réel. Cet article étudie le problème de savoir comment router les données à partir de la source jusqu'à la destination afin de maximiser la probabilité de livraison dans un délai donné. Nous supposons que nous connaissons les horaires de bus, mais nous prenons en compte le caractère aléatoire de la mobilité des bus, dû aux conditions de circulation ou au temps nécessaire pour l'embarquement et le débarquement des passagers. En ce sens, le présent document est l'un des premiers à aborder un scénario de mobilité quasi-déterministe. Nous proposons un modèle stochastique simple pour les arrivées de bus aux arrêts, motivé par une étude des traces réelles recueillies dans un vaste réseau urbain avec 250 lignes de bus et environ 7500 arrêts de bus. Une représentation graphique succincte de ce modèle nous permet de concevoir un algorithme de routage optimal (conformément à notre modèle) utilisant une seule copie des données, puis de l'étendre au cas où plusieurs copies des mêmes données sont permises. Grâce à une vaste étude de simulation, nous comparons l'algorithme de routage optimal avec trois autres approches : minimiser le temps attendu de traversement du graphe, maximiser la probabilité de livraison sur un horizon temporel infini, et un algorithme heuristique récemment proposé basé sur les fréquences de bus. Nous montrons que, en général, notre algorithme optimal surpasse les trois autres, mais il se réduit essentiellement à minimiser le temps de traversement quand les transmissions sont toujours couronnées de succès, ou à maximiser la probabilité de livraison sur un horizon temporel infini lorsque les transmissions échouent fréquemment. Pour les transmissions fiables et des valeurs des délais «raisonnables», l'extension multi-copie nécessite seulement 10 copies pour atteindre quasiment la même performance que celle du flooding, particulièrement coûteux en terme de nombre de transmissions et utilisation de buffers.

**Mots-clés :** French Keywords

# 1 Introduction

We consider an opportunistic data network formed by (some) buses and bus stops equipped with wireless devices, e.g. based on WiFi technologies, like in DieselNet [13]. Most of the stops act as disconnected relay nodes (the throwboxes in [3]), and a few of them are also connected to the Internet. Data are delivered across town following the *store-carry-forward* network paradigm [44], based on multi-hop communication in which two nodes may exchange data messages whenever they are within transmission range of each other.

A bus-based network is a convenient solution as wireless backbone for delay tolerant applications in an urban scenario. In fact, a public transportation system provides access to a large set of users (e.g. the passengers themselves), and is already designed to guarantee a coverage of the urban area, taking into account human mobility patterns. Moreover, such a wireless backbone is not significantly constrained by power and/or memory limitations: a throwbox can be easily placed on a bus and connected to its power supply, or be put in an appropriate place in bus stops, which are usually already connected to the power grid to provide lights and electronic displays, but also in any other places where power supply is available. Finally, travel times can be predicted from the transportation system time-table; even if the actual times are affected by varying road traffic conditions and passengers' boarding and alighting times, such a backbone still provides strong probabilistic guarantees on data delivery time that are not common in opportunistic networks.

Indeed, this paper explores the basic question: “*how to route data over a bus-based network, from a given source to a given destination, so that the delivery probability by a given deadline is maximized?*”. We rely on the knowledge of bus schedule information and some stochastic characterization of bus mobility, obtained from real data traces.

We consider two classes of routing schemes over such a network. The first class relies only on forwarding a *single copy* of the data is propagated along a *single path*. The second class takes advantage of *multiple copies* spread in the network to increase delivery probability and reduce delivery time, albeit with higher bandwidth usage.

Another architectural choice is between exploiting only bus-bus contacts, only bus-stop contacts, or both types of contacts. While the latter case should provide better performance, the two kinds of transmission opportunities have very different characteristics, making it hard to model both of them together in a common framework. For example, a potential contact between two buses traveling along orthogonal trajectories can be *completely avoided* if there is even a slight delay of one of them. On the other hand, in case of a bus-stop communication, the contact always happens eventually, but may be delayed. Most prior art (see Sec. 2) considered only bus-bus communications. In this paper, we focus on the other alternative, relying only on *bus-stop* communications. In Appendix A, we show that bus-stop communications potentially offer better performance in the real bus network scenario under consideration. Further, we present an analysis on connectivity of the bus network using the bus-stop communications in Appendix E.

Fig. 1 depicts the high-level framework used in the paper to study routing in the proposed network. Our starting point is a simple mobility model for buses (described in Sec. 3.1), that is supported by the statistical analysis of a set of real traces of the public transportation system of Turin in Italy, which serves an area of about 200 km<sup>2</sup> through about 7500 stops and 1500 vehicles distributed among 250 lines. These traces include the complete schedule for a working day and the corresponding GPS traces with the positions of all the vehicles during the morning rush hour period (6 AM–10 AM).

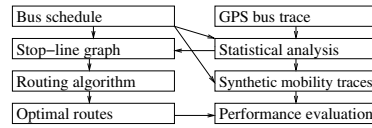


Figure 1: High-Level Evaluation Framework

A statistical analysis of these traces in Sec. 3.1 yields some important conclusions, that allow us to represent the transportation system appropriately in terms of a graph with independent random weights, that we call the *stop-line graph* (Sec. 4). Under this representation, our original optimization problem to identify routes maximizing the delivery probability by a given deadline (or maximizing the on-time delivery probability) becomes equivalent to a specific stochastic shortest path problem on the stop-line graph. We are able to find an optimal algorithm, called ON-TIME, for the single-copy case (Sec. 4.2) and then to extend it for the multi-copy case through a greedy approach (Sec. 4.4). We compare the performance of these proposed algorithms with three other heuristics (Sec. 4.3) that also operate on the stop-line graph: an adaptation of the routing algorithm proposed in [38] for bus-bus communications (we refer to it as MIN-HEADWAY), and the two naïve algorithms, MIN-DELAY, that determines the path with the least expected weight, and MAX-PROB, that maximizes the delivery probability on an infinite time-horizon. Since the number of real-life traces we obtained is limited, the comparison (Sec. 5) is based on simulations carried on a large set of synthetic traces generated on the basis of our bus mobility model and the schedule of Turin bus system.

The paper has the following main contributions and conclusions.

1. Formulation of the original routing problem as a specific stochastic shortest problem on a particular stochastic graph, that is justified by a statistical analysis of real transportation system traces.
2. Optimal (under our model) routing scheme for the single copy case. While this offline routing scheme has, in theory, an exponential worst-case time complexity, in practice it is able to find the optimal route in reasonable time, allowing each node to store an optimal pre-selected routing plan.
3. Extensions to multi-copy case, based on greedy approaches applied to the single-copy scheme. We prove a tight bound of  $1/k$  for the on-time delivery probability in comparison to an optimal (non-greedy)  $k$ -copy scheme.
4. Simulation analysis showing that the optimal algorithm outperforms the MIN-HEADWAY heuristic, but it performs as the MIN-DELAY algorithm when there is no packet loss, and as MAX-PROB when packet losses are significant across the network. We provide some explanation for these results. In this sense the conclusion is that naïve heuristics like MIN-DELAY or MAX-PROB algorithms may be very good heuristics for routing over realistic bus transportation networks.
5. Simulations showing that only 10 copies are needed for a multi-copy greedy approach to reach performance close to flooding routing policies; the latter requires at least two order of magnitude more transmissions and copies for each single piece of data.

## 2 Related Work

Employing a bus network as a mobile backbone for dense vehicular networks was first proposed in [47], using standard routing protocols for mobile ad-hoc networks (e.g., DSR or AODV). More recently, buses employment in a disconnected scenario has been considered; e.g. in the seminal *DieselNet* project [13]. Since our paper considers routing in such a network, in what follows we only mention work related to routing issues.

Most of the research has focused on bus-bus communications [10, 2, 38, 17, 18] with the following routing approach: Each vehicle learns at run time about its meeting process; then, the vehicles exchange their local view with other vehicles and use the information collected to decide how to route data. The goals of the proposed algorithms were either to reduce the expected delivery time or to maximize the delivery probability. Unlike these studies, we mainly focus on *bus to stop data transfers* and derive a single-copy routing algorithm to maximize the delivery probability by a given deadline. We then extend the algorithm to address settings where several copies of the same data are permitted. On the other hand, we do not consider buffer or bandwidth constraints, (e.g., as in [10, 2]) as they are not a major concern in our settings: When the mobile devices are buses (as opposed, for example, to cellular phones), it is reasonable to assume that there is sufficient storage available; in addition, since buses communicate with stops (as opposed to other moving buses), the amount of data transferable during a meeting is larger. Nevertheless, characterizing the bandwidth of the contacts and incorporating these constraints into our framework for bandwidth-hungry applications is part of our ongoing research.

The use of fixed relay nodes was also considered in [5, 3]. In [5], an architecture is proposed where bus passengers may use the cellular network to require content that will be delivered to access points along the bus trajectory. This data can be replicated also on other buses, taking advantage of possible data transfers between vehicles. Their analysis considers only a simplistic single-street scenario and does not address routing issues. [3] reports that the performance of a vehicular network is improved by adding some infrastructure, like base stations connected to the Internet, a mesh wireless backbone, or fixed relays (which are similar to our stops). The most important results are (i) there are scenarios where a mesh or relay hybrid network is a better choice over a base station networks; (ii) deploying some infrastructure has a much more significant effect on delivery delay than increasing the number of mobile nodes. These findings, which were verified both analytically and by experiments on DieselNet testbed, support our proposed architecture that relies on an opportunistic connectivity between vehicle nodes and fixed relays.

In order to provide low cost Internet connectivity to fixed kiosks in rural areas of developing counties, KioskNet architecture has been proposed [21]. In this architecture, buses carry data between the kiosks and a set of gateways that can communicate to a proxy on the Internet. Routing of such data is achieved by simple flooding. On the other hand, gateways are delegated to a kiosk via a scheduling mechanism that considers the schedule of the buses which serve the kiosk [22].

The routing algorithms proposed by [28, 29, 30, 31] are intrinsically more suited for bus to bus data transfers. [29] and [31] propose algorithms that take advantage of cyclic mobility patterns, according to which nodes meet periodically, albeit with some probability. Even if a given bus may meet multiple times the same stop, this approach does not fit our scenario for three reasons. First, the bus-stop contact process is not necessarily periodic because vehicles may be assigned to different lines during one operation



day. Second, even if a vehicle operates always on the same line, its frequency changes significantly along the day. Third and more importantly, even when a period may be defined, its time duration ranges from 30 minutes to 2 hours (depending mainly on the length of the bus trajectory and on inactivity times at terminus), and it is then comparable with the deadlines we are targeting, so that it is not possible to take advantage of such long term periodicity. Other forms of long-term regularities in the contact process of the different nodes [30] are too general for our settings, since we have significantly more information on the meetings that can be exploited to improve the performance. Finally, [28] proposes hierarchical routing for a deterministic network, whereas we consider non-deterministic mobility.

Almost all the papers above have considered only small bus networks (40 buses for DieselNet, 16 buses on a cyclic path for MobTorrent [5]). Only [17] considers an urban setting with a public transportation system comparable to ours (70 different bus lines), but, differently from us, they do not use any real mobility trace and simulate bus movement assuming that the bus speed is chosen uniformly at random from a given interval.

From the theoretical point of view, our optimization goal can be reformulated (under some assumptions) as a particular *stochastic shortest path problem* that deals with a graph  $G$  whose edge lengths (or equivalently, traversal times over the edges) are random variables. Several optimality criteria were considered in the past for routing in stochastic graphs. The most common one is the *least expected traversal time*, which can be generalized to any linear (or affine) utility function [46, 37]. Other optimality criteria are deviance [7], monotonic quadratic utility functions [9] and prospect-theory-based functions [25]. Recent and comprehensive surveys of the different utility functions and corresponding solutions appear in [36, 8]. Our paper deals with the *reliability* of the chosen path, namely, finding a path which maximizes the probability of on-time arrival (given some deadline). This problem was first studied by Frank [16] and then was also investigated in [34, 32, 33] and more recently in [14, 15, 35, 36]. Current state-of-the-art algorithms still have exponential worst-case time complexity, based on enumerating over some set of candidate paths [36].

Yet, our problem differs from Frank's problem essentially in three aspects. First, we have considered a real transportation system and therefore we are not interested in the worst-case complexity of some general graphs. Second, our transportation model has two kinds of entities: stations and buses; we need to take into account waiting time at the stops and not only buses travel times, as explained in details in Sec. 4. Third, all the previous work considered a single-copy model, while our model deals also with multiple copies where the objective is that at least one of the copies arrives at the destination before the deadline.

Finally, we observe that we use the bus network for data transfer as it is used for passenger transfer. Thus, one could expect that the same problem has already been addressed in the transportation literature. However, this is not the case: First, the possibility to exploit multi-copy is clearly absent in the transportation of people or merchandise. Second, the probability to miss a transfer opportunity is also not considered in transportation, while data transfer between two nodes may fail because of insufficient contact duration, channel noise or collisions. Third, even for single-copy routing, bus network passenger routes usually aim to *minimize the expected traversal time* (possibly limiting the maximum number of bus changes) and not to maximize the delivery probability by a given deadline, as we are doing (cf. [45, 6, 11] and references therein). The fact that finally minimizing the expected traversal time may provide almost optimal performance in some scenarios is an a-priori unexpected finding of this research.

In conclusion, to the best of our knowledge, this is the first paper that proposes an optimal routing algorithm that takes advantage of bus schedule information as well as a stochastic characterization of bus mobility, supported by real data traces.

### 3 Model Definitions and Assumptions

In this section, we formally define the terms and notations we use to describe a transportation system, following the terminology used in transportation literature.

A transportation system  $\mathcal{T}$  has a set of stops, denoted by  $\mathcal{S}$ , and a set of vehicles (buses), denoted by  $\mathcal{V}$ , which travel between the stops according to a predetermined path and a predetermined schedule. For each vehicle  $v \in \mathcal{V}$ , the schedule allows us to determine its *trajectory*, denoted  $\text{traj}(v)$ , which is the ordered sequence of stops the vehicle traverses:  $\text{traj}(v) = (s_0, s_1, \dots, s_n)$ . In addition, each vehicle  $v$  is associated with a *trip*, denoted  $\text{trip}(v)$ , which is a time-stamped trajectory:

$$\text{trip}(v) = ((s_0, \tau_0), (s_1, \tau_1), \dots, (s_n, \tau_n)),$$

such that a vehicle  $v$  should arrive at stop  $s_i$  along its trajectory at time<sup>1</sup>  $\tau_i = \tau(v, s_i)$ . We distinguish between the scheduled time  $\tau_i$  and the actual time  $t_i = t(v, s_i)$ , which is a random variable depending on road traffic fluctuations, passengers boarding and alighting, etc. The difference between the actual arrival time  $t(v, s_i)$  at a stop  $s_i$  and its corresponding scheduled arrival time  $\tau(v, s_i)$  is the *lateness*  $l(v, s_i)$  of the vehicle at stop  $s_i$ :  $l(v, s_i) = t(v, s_i) - \tau(v, s_i)$ . Note that the lateness is negative when the vehicle arrives earlier than its scheduled arrival. The *delay*  $d(v, s_i, s_j)$  between the stops  $s_i$  and  $s_j$  is the change in the lateness:  $d(v, s_i, s_j) = l(v, s_j) - l(v, s_i)$ . The time difference between the arrivals of a vehicle at two different stops  $s_i$  and  $s_j$ , is called the *actual travel time* between the two stops,  $tt(v, s_i, s_j) = t(v, s_j) - t(v, s_i)$ . The scheduled travel time is simply the difference between the scheduled arrivals at the two stops.

A key concept in bus networks is the notion of *lines*, which are basically different vehicles with the same trajectory (at different times). Let  $\mathcal{L}$  denotes the set of lines. For each vehicle  $v \in \mathcal{V}$  we denote its corresponding line by  $\text{line}(v) = \{v' \in \mathcal{V} | \text{traj}(v) = \text{traj}(v')\}$ . Note that lines introduce an important characteristic of a bus transportation system: if a passenger misses a specific vehicle  $v$ , she can still catch another vehicle  $v'$  in  $\text{line}(v)$  and reach the same set of stops. The time between two consecutive arrivals of vehicles belonging to the same line at the same stop is called *headway*.

In the sequel, we will refer to the transportation system  $\mathcal{T}$  as the quintuple  $\langle \mathcal{S}, \mathcal{V}, \mathcal{L}, \tau(), t() \rangle$ , where the function  $\tau()$  is a way to represent the schedule and  $t()$  denotes a characterization of the stochastic process of vehicle arrivals at the stops. In the next section, we are going to start characterizing this stochastic process.

#### 3.1 Bus Mobility and Communication Models

The problem of maximizing the delivery probability by a given deadline requires a realistic statistical characterization of bus mobility patterns, which is also useful to generate a large set of synthetic traces and evaluate the performance of our routing algorithms.

<sup>1</sup> We do not introduce explicitly a departure time from the stop, because in our paper we do not take into account bandwidth constraints so that it is not important to specify the duration of the transmission opportunity between a bus and a stop. Moreover from our traces it is possible to determine the arrival time, but not the departure time.

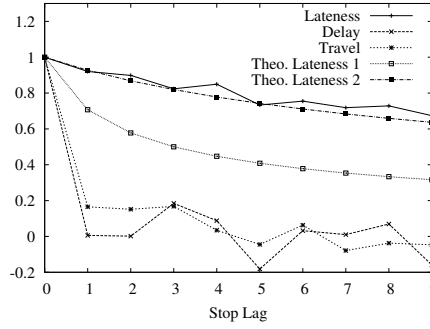


Figure 2: Autocorrelation functions for lateness, delay and travel time.

Transportation literature does not provide a universally valid model for bus movements in an urban environment, since they are strongly affected by vehicular and passenger traffic conditions, road organization (availability of separate lanes for buses), traffic signal control management (priority may be given to the approaching buses over the other traffic), company policies (penalties to the bus drivers for delays), and so on; details of our transportation literature survey are in Appendix B. Two extreme cases can be considered: 1) buses that are late at one stop can always recover their delay at the following stop (speeding up and reducing their travel times), 2) buses move almost in the same way, and they do not try to recover their delay. The first case better describes lines with high headway, while the second is probably more adapt for lines with short headways, where buses try to respect a given frequency, rather than an exact schedule<sup>2</sup>. In terms of the quantities we have defined above, in the first case, latenesses at consecutive stops are almost independent, while in the second case they are highly correlated.

We have performed a statistical analysis of a one day trace with actual bus arrivals at their stops provided to us by Turin's public transportation company. Their network consists of around 250 lines (which includes mainly buses, but also trams and subway trains) and a fleet of almost 1,500 vehicles. Some manual inspection is needed to be able to assign specific trip to their schedule (in order to evaluate metric like the lateness), so that we worked on a subset of the trace, consisting of 6 lines in both direction, with a total of 408 trips and 11,097 arrivals at bus stops.

Fig. 2 shows the empirical autocorrelation function for lateness, delay, and travel time. In particular, we have considered for each vehicle the sequence of latenesses at consecutive stops<sup>3</sup> ( $l(s_0), l(s_1), \dots, l(s_n), \dots$ ), the sequence of delays between consecutive stops ( $d(s_0, s_1), d(s_1, s_2), \dots, d(s_n, s_{n+1}), \dots$ ) and the sequence of travel times between consecutive stops ( $t_1 - t_0, t_2 - t_1, \dots, t_{n+1} - t_n, \dots$ ). We have assumed that the sequences (relative to the same quantity) obtained for different vehicles are samples of the same random process, and we have used them to evaluate the empirical autocorrelation function. Fig. 2 demonstrates that the lateness values at consecutive stops are highly correlated. It is then clear that a simplistic bus mobility model, where the actual arrival time of vehicle  $v$  at stop  $s$  is equal to the schedule one plus some independent noise ( $t(v, s) = \tau(v, s) + n(v, s)$ ), is unrealistic. At the same time, we note

<sup>2</sup> This distinction is expressly advertised by Turin public transportation system, that label lines as frequency-based and schedule-based.

<sup>3</sup>With a slight abuse a notation, we omit the dependence on vehicle  $v$ , when it is clear from the context.

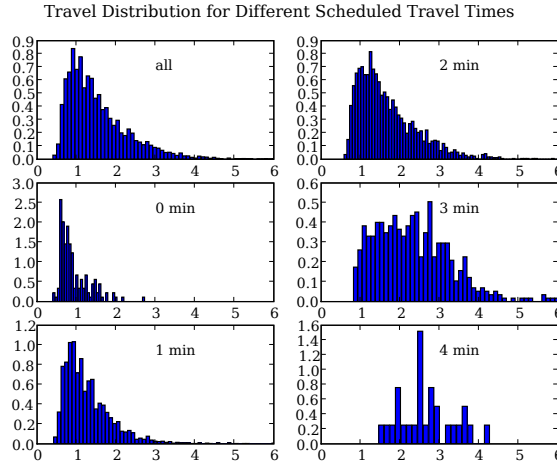


Figure 3: Travel time distribution (aggregated and for different scheduled travel times).

that delays and travel times are significantly less correlated; this suggests the following model, in terms of travel time:

$$t(v, s_k) = \tau_0 + l(s_0) + \sum_{i=0}^k tt(v, s_i, s_{i+1}), \quad (1)$$

where we can assume that travel times are random variables.

If we assume that delays are independent and identically distributed and that the lateness at the first stop  $l(s_0)$  is distributed as  $d(s_i, s_{i+1})$ , it is possible to evaluate analytically the expression of the autocorrelation function. This is represented in Fig. 2 by the curve “theoretical lateness 1”. We note that there is still a strong part of the correlation to be justified. A specific analysis of the lateness at the first stop shows that  $l(s_0)$  is not distributed as  $d(s_i, s_{i+1})$ , and moreover its variance is almost 6 times larger. This shows that the variability of vehicle departure times is a significant component of the variability of arrival times at following stops. If we correct the expression of the autocorrelation function taking into account this empirical finding, we can obtain the new curve “theoretical lateness 2” that matches the empirical one very well.

As a conclusion of this statistical analysis, we are going to assume in the rest of the paper that

**Assumption 1.** *Bus travel times at consecutive stops are independent (but not necessarily identically distributed; in particular, their distribution will depend on the corresponding scheduled value).*

We continue our statistical analysis by determining realistic distributions for the lateness at the first stop  $l(s_0)$  and the delay distribution, in order to completely characterize the random variables of Eq. (1). This also allows us to use this recursive formula to generate realistic random traces (See Appendix C). For example, Fig. 3 shows the empirical distribution of the travel times (assumed to be homogeneous across different lines) when all the samples are aggregated and when they are split by the corresponding scheduled travel times. It is evident that different distributions have to be used,

depending on the different scheduled travel times. Since it is quite common in transportation literature to use the lognormal distribution to model travel times, we have adopted this trend and characterized the parameters of the lognormal distributions for different scheduled travel times by moment matching techniques.

Our second assumption concerns the waiting time at a stop when commuting from one line to another:

**Assumption 2.** *The distribution of the waiting time at a stop only depends on the stop and the characteristic of the departing bus line, not on the arrival line.*

We note that Assumption 2, which plays an important role in enabling a graph representation with additive edge weights, is partially a consequence of Assumption 1: Consider buses moving according to the schedule, and transferring from line  $\ell_1$  to line  $\ell_2$  at stop  $s$ . It is clear that the waiting time at the stop can be evaluated a-priori on the basis of the scheduled arrival time of the  $\ell_1$  vehicle and the departure time of the following  $\ell_2$  vehicle. But under Assumption 1, arrival times of  $\ell_1$  buses at stop  $s$  are random variables and so are the corresponding waiting times. Intuitively, if the variability of  $\ell_1$  arrival times is large in comparison to the headway<sup>4</sup> of line  $\ell_2$ , the waiting time will have almost the same distribution of the waiting time seen by a Poisson observer, thus it is independent of  $\ell_1$ 's schedule.

Finally, in our scenario we assume that data transfer during a transmission opportunity can fail. This can be due to different causes: channel noise and collisions, but also nodes failing to discover the opportunity, or contact duration being insufficient to transfer the data. Our main assumption is the following:

**Assumption 3.** *Message success probabilities of different contacts are independent.*

## 4 Routing Algorithms in a Bus Network

As mentioned before, our routing algorithms aim to define an off-line routing for the transportation system that maximizes data delivery probability by a given deadline:

**Definition 1.** *Given a transportation system  $\mathcal{T} = \langle \mathcal{S}, \mathcal{V}, \mathcal{L}, \tau(), t() \rangle$ , a source stop  $s_s$ , a destination stop  $s_d$ , a start time  $t_{start}$ , and a deadline  $t_{stop}$ , the on-time delivery problem is to find a route between  $s_s$  and  $s_d$  that starts after time  $t_{start}$  and maximizes the on-time delivery probability, i.e.  $\Pr\{\text{data is delivered before time } t_{stop}\}$ .*

We first discuss how we represent the transportation system as a graph, considering the natural operation of a bus system with transfers from buses to stops and then to buses (i.e., involving only bus-stop communications). The following four issues lead to our final representation: computational complexity, intrinsic properties of the bus transportation system (namely, the existence of lines), characteristic of the stochastic process  $t()$  (namely, waiting times in the stops depends on the departing line), and an advantage coming from working with additive edge weights.

### 4.1 Methodology

A simple way to represent the transportation system  $\mathcal{T}$  is by a *temporal network* [26], that is a multi-graph whose set of nodes consists of  $\mathcal{S} \cup \mathcal{V}$  (i.e., a node for each vehicle

<sup>4</sup>According to our model the variance of the lateness increases along the trajectory.

and for each stop) and each edge represents a transmission opportunity between a vehicle  $v$  and a stop  $s$  (or vice versa) occurring at the time instant  $t(v, s)$  and can therefore be represented by the triple  $\langle v, s, t(v, s) \rangle$  (or  $\langle s, v, t(v, s) \rangle$ ). A possible route in such graph would then be a path connecting the source  $s_s$  and the destination  $s_d$ , i.e. a sequence of edges, like  $(\langle s_s, v_0, t(v_0, s_s) \rangle, \langle v_0, s_1, t(v_0, s_1) \rangle, \langle s_1, v_1, t(v_1, s_1) \rangle, \dots, \langle v_n, s_d, t(v_n, s_d) \rangle)$ . This route is able to deliver the data from  $s_s$  to  $s_d$ , only if  $t_{start} \leq t(v_0, s_s) \leq t(v_0, s_1) \leq t(v_1, s_1) \leq \dots \leq t(v_n, s_d) \leq t_{stop}$ . We observe that a data transmission failure can be incorporated in this model simply by considering that the corresponding event time is infinite.

While the temporal network is useful for deterministic scenarios, it is not suitable for the transportation system we are considering. The first reason is that in a large-scale transportation network, this graph would have a very large number of nodes ( $|\mathcal{S} \cup \mathcal{V}|$ ) and of edges. For example if the time interval  $[t_{start}, t_{stop}]$  spans a few hours, a stop in a dense traffic can exhibit hundreds of edges. The second reason is that it ignores the fact that in a bus network a vehicle in such route can be in some sense “replaced” by another vehicle of the same line. Finally, given our performance metric, we would need to evaluate  $\Pr\{t_{start} \leq t(v_0, s_s) \leq t(v_0, s_1) \leq t(v_1, s_1) \leq \dots \leq t(v_n, s_d) \leq t_{stop}\}$ . However, the results of Sec. 3.1 show that lateness values at consecutive stops are strongly correlated, making it impossible to simply evaluate this probability.

For these reasons it appears more beneficial to directly look for routes from the source to the destination in terms of lines. We can consider an alternative data structure, the *line-based graph*  $G_{lines} = \langle \mathcal{S}, E_{lines} \rangle$ , in which nodes are bus stops and there is an edge between two stops  $s_i$  and  $s_j$  if and only if there is a line  $\ell \in \mathcal{L}$  that goes from  $s_i$  to  $s_j$  (only stops which are served by at least two lines need to be considered). It is important to notice an intrinsic difference between the vehicular DTN and the line-based graph: in the vehicular DTN graph we check the feasibility of the path, by evaluating the probability that it maintains the chronological order between contacts. On the other hand, in the line-based graph, the paths are always feasible and we are interested to check whether their total length (that is, the total traversal time of the path) is less than  $t_{stop} - t_{start}$ . Note that the traversal-time along a specific path is a random variable which is the sum of two kinds of random variables: edge random variables, which captures how travel time between two specific stops on a specific line is distributed, and node random variables, which captures the distribution of the waiting time at the stops.

The waiting time at a stop poses a major difficulty on the design of a routing algorithm, because it is not simply related to the stop but it depends on the specific route under consideration, and more specifically on the stop’s outgoing and incoming edges in the route. For example, if both edges correspond to the same line, the waiting time at the stop is 0. On the other hand, when switching lines at the stop, the waiting time depends only on the *headway* of the departing line by Assumption 2.

In our representation, which we call *stop-line graph*  $G_{sl} = \langle V_{sl}, E_{sl} \rangle$ , the nodes are  $(s, \ell)$  pairs where  $s$  is a stop and  $\ell$  is a line;  $(s, \ell) \in V_{sl}$  if and only if line  $\ell \in \mathcal{L}$  arrives (or depart) at stop  $s \in \mathcal{S}$ . In addition, we add two nodes  $s_s$  and  $s_d$  which are connected to all nodes that correspond to the source and destination stops. The edges of  $G_{sl}$  are defined as follows: An edge between  $(s, \ell)$  and  $(s', \ell')$  corresponds to routes between stops  $s$  and  $s'$  with line  $\ell$  that continue from stop  $s'$  on line  $\ell'$ . If  $\ell = \ell'$  we call the edge a *travel edge*, while if  $\ell \neq \ell'$  we call it a *travel-switch edge*. An example of  $G_{sl}$  appears in Fig. 4.

We now define the random variables associated to the edges in  $E_{sl}$ . The random variable of a travel edge describes the corresponding travel time between two stops:



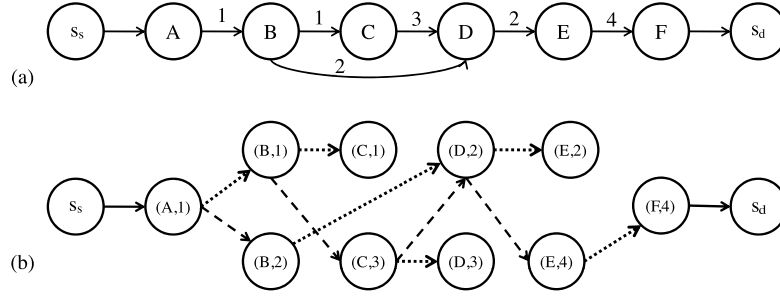


Figure 4: (a) Example of bus network with  $\mathcal{S} = \{A, B, C, D, E, F\}$  and  $\mathcal{L} = \{1, 2, 3, 4\}$ : the node corresponds to a stop and the label on the edge represents the line connecting the two stops. (b) The corresponding line-stop graph  $G_{sl}$ . Dotted edges are travel edges, while dashed edges are travel-switch edges.

formally, a travel edge  $e = ((s, \ell), (s', \ell))$  is associated with the random variable  $w_e = tt(\ell, s, s')$  describing the travel time of a line  $\ell$  bus from stop  $s$  to stop  $s'$ . The random variable of a travel-switch edge includes the travel time between the corresponding stops and the waiting time for the next line, taking into account possible transmission failures. Formally, a travel-switch edge  $e = ((s, \ell), (s', \ell'))$  is associated with the following random variable  $w_e$ .

$$w_e = \begin{cases} +\infty & \text{with prob. } p_f \\ tt(\ell, s, s') + wt(\ell', s', k) & \text{with prob. } (1 - p_f)^2 p_f^{k-1} \end{cases}$$

for any  $k \geq 1$ ; here,  $p_f$  is the transmission failure probability and  $wt(\ell', s', k)$  is the waiting time at stop  $s'$  before the arrival of the next  $k$ th bus of line  $\ell'$ . Note that, to be able to switch the data successfully from one bus to another, two transmissions must succeed: the one from a bus of  $\ell$  to  $s'$  and the one from  $s'$  to a bus of  $\ell'$ . We assume that all the random variables defining  $w_e$  are known (they will be characterized in Sec. 4.2); moreover, by Assumptions 1, 2 and 3, they are all independent.

It is important to notice that the stop-line pair representation provides a unified approach to deal with waiting times at the stops, thus solving shortcoming in previous approaches (e.g., temporal network [26], or graphs with stops as nodes and lines as edges); further, although out of the scope of this paper,  $G_{sl}$  is also usable in settings where Assumption 2 does not hold.

Our model allows us to define simply the overall traversal time of the data along a weighted path  $\mathcal{P}$  as:  $tr(\mathcal{P}) = \sum_{e \in \mathcal{P}} w_e$ . Note that  $p_f$  introduces a scaling factor equal to  $(1 - p_f)$ , for each transmission from the bus to the stop, on the final Cumulative Distribution Function (CDF) of the delivery time. Now, given the graph  $G_{sl}$ , the on-time delivery problem corresponds to finding a path  $\mathcal{P}$  such that  $\Pr\{tr(\mathcal{P}) \leq t_{stop} - t_{start}\}$  is maximized. Note that, under this construction, our problem is similar to the problem defined by Frank [16], with the differences highlighted at the end of Sec. 2.

## 4.2 Single-Copy Routing Algorithm and Implementation

We now turn to define our routing algorithm, called ON-TIME, which aims at solving the on-time delivery problem. ON-TIME finds, in general, different paths for different values of (relative) deadline  $t_{stop} - t_{start}$ . For example, Fig. 5 compares the Cumulative Distribution Functions (CDF) for the delivery times of 3 different paths, for a given

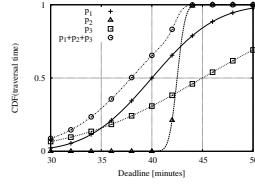


Figure 5: Delivery probability CDFs of three disjoint paths  $P_1$ ,  $P_2$  and  $P_3$ , connecting a source and a destination with different traversal times and without transmission failures ( $p_f = 0$ ). Path  $P_1$  has the lowest expected traversal time; the variance of  $P_2$  is the smallest, while  $P_3$ 's variance is the largest.  $P_1$ ,  $P_2$  and  $P_3$  are respectively the optimal paths computed by ON-TIME for deadlines between 34 and 43 minutes, larger than 43 minutes, and shorter than 34 minutes. The curve labeled  $P_1 + P_2 + P_3$  corresponds to the success probability obtained by a multi-copy approach exploiting all the three paths.

source-destination pair and no transmission failures ( $p_f = 0$ ). In this case, ON-TIME chooses one of the three paths depending on the given deadline. Nevertheless, the larger the deadline, the larger the resulting on-time delivery probability is.

ON-TIME works by first determining a potentially good path between the source to the destination (for example, that with the minimum expected traversal time), and evaluating its on-time delivery probability. This can be done by performing a (numerical) *convolution* of the different random variables distributions along the path, yielding the end-to-end traversal time distribution. By this distribution, it is then easy to calculate (using the corresponding CDF) the delivery probability by the deadline.

Then, the algorithm proceeds by exploring the graph through a breadth-first search, looking for paths with a higher on-time delivery probability. A *pruning* mechanism avoids the need to determine and evaluate all the paths. By the associativity of the convolution operator and the fact that our random variables are all non-negatives, for any path  $\mathcal{P}$  and any prefix  $\mathcal{P}'$  of  $\mathcal{P}$ ,  $\Pr\{tr(\mathcal{P}) \leq t\} \leq \Pr\{tr(\mathcal{P}') \leq t\}$ . Thus, we can perform hop-by-hop convolution and compute, for each resulting distribution, the probability that the weight (that is, traversal time) of this path's prefix is less than  $t_{stop} - t_{start}$ ; if the probability is smaller than that of the current best path, there is no need to consider the rest of the path. From a practical point of view, working with a real transportation network, this simple pruning mechanism significantly reduces the number of paths to be considered, even if theoretically we may have a factorial number of paths to explore.

In our implementation, we have introduced some other simplifications, which reduce the computation time, but, at the same time, may lead to suboptimal paths. First, we have introduced a limit  $h$  of the exploration depth during the search. Given  $h$  as a constant, the algorithm is then guaranteed to run in polynomial time. We observe that upon termination, we may be able to say if the algorithm has selected the optimal path or there may be a better one. In fact, when we stop, if there is still some path prefix of length not larger than  $h$  such that the pruning mechanism cannot discard it, then there could be a longer path with higher on-time delivery probability. But if this is not the case, then the current best candidate is actually the optimal path. In our experiments on Turin transportation network,  $h = 8$  was enough to find all the best paths. Although this value may change for other networks, we expect that it will remain a relatively



small constant. Note that a suitable  $h$  for each network can be found by conducting experiments similar to ours.

A second simplification is that we restrict the set of eligible paths such that each line can be used only in consecutive edges. This prevents the algorithm to explore paths using line  $\ell_1$  then line  $\ell_2$ , and then again line  $\ell_1$ . We expect that these paths have normally worse performance than those where data message just remains on line  $\ell_1$ .

Finally, we have avoided the computation burden of performing numerical convolution by assuming that the end-to-end traversal time, which is a sum of independent random variables, can be approximated by a normal distribution. In this case, it is sufficient to take into account the mean and the variance of each edge weight, conditioned on the fact that it is finite (respectively,  $\mu_e = E[w_e | w_e < \infty]$  and  $\sigma_e^2 = \text{Var}[w_e | w_e < \infty]$ ), and the probability that the edge weight is finite (denoted by  $p_e$ ). Then, the CDF of the traversal time of path  $\mathcal{P}$  is equal to the CDF of a normal distribution with mean  $\sum_{e \in \mathcal{P}} \mu_e$  and variance  $\sum_{e \in \mathcal{P}} \sigma_e^2$ , multiplied by a scaling factor  $\prod_{e \in \mathcal{P}} p_e$ . In the case of travel edges, average and variance of  $tt(\ell, s, s')$  can be measured directly on the traces. In the case of travel-switch edges, we have to also to evaluate the average and variance of  $wt(\ell, s, k)$  using the first three moments of the interarrival times of the line  $\ell$  buses to stop  $s$  (which can be also measured on the traces) and some basic Palm calculus. For example, assuming perfect periodic bus arrivals with period  $\delta$  and failure probability  $p_f$ ,  $E[wt(\ell, s, k)] = \delta(1/2 + p_f/(1 - p_f))$  and  $E[wt(\ell, s, k)^2] = \delta^2(1/3 + 2p_f/(1 - p_f)^2)$ . Note that these values can be computed for the specific arrival process observed in bus traces.

In what follows, we evaluate the performance of ON-TIME for different source-destination pairs under similar kind of deadlines. If we had fixed a given deadline for all the pairs, then this deadline could be unfeasible for some of them (in the sense that there is no way to deliver the message by this deadline, e.g. if the deadline is smaller than the time a vehicle would take to move from the source to the destination), and trivially satisfiable for other pairs (many different paths would deliver with probability almost one). For this reason, given a source  $s_s$ , a destination  $s_d$  and a real value  $x \in [0, 100]$ , let  $\phi(x, s_s, s_d)$  be the deadline  $t_{stop}$  for which the on-time delivery probability of the path from  $s_s$  to  $s_d$  with minimum expected traversal time is  $x\%$  (assuming  $p_f = 0$ ). We denote by ON-TIME( $x$ ) the on-time routing algorithm where the deadline is set equal to  $\phi(x, s_s, s_d)$  for every source-destination pair  $(s_s, s_d)$ . Intuitively, the smaller  $x$  is, the “shorter” the deadlines are considered, where “short” is in relation to the expected traversal time from  $s_s$  to  $s_d$  and not in an absolute sense.

### 4.3 Other Routing Approaches

Although the algorithm we described is optimal under our model assumptions, we also consider sub-optimal but simpler heuristics.

The most intuitive approach (denoted as MIN-DELAY) is to route in  $G_{sl}$  along the path whose expected traversal time is minimal. Note that MIN-DELAY is equivalent to ON-TIME(50) under the Gaussian assumption on the distribution of the traversal time. Fig. 5 shows that path  $P_1$ , found by MIN-DELAY, does not always correspond to the highest on-time delivery probability. On the other hand, MIN-DELAY is computationally attractive, because the path with the least expected traversal time can be easily computed with Dijkstra’s algorithm (by linearity of expectation). In Sec. 5, we compare our optimal algorithm to this sub-optimal heuristic and show that it often suffices to use this simple approach.

A second algorithm, MAX-PROB, selects the path that maximizes the delivery probability on an infinite time-horizon. Also this path can be determined running Dijkstra's algorithm on the line-stop graph with edge weights equal to  $-\log(p_e)$ . MAX-PROB and ON-TIME tend to select the same path, for low transmission success probabilities, as shown at the end of Sec. 5.

Another approach, denoted MIN-HEADWAY, tries to minimize the sum of all lines headways along a path [38], thus preferring frequent lines over infrequent ones; it was proposed originally for bus-to-bus communications. In Sec. 5, we show that it has the worse performance in our settings among all the different algorithms.

#### 4.4 Extension to Multi-Copy Routing

As shown in the toy-case of Fig. 5, using a multi-copy scheme (the curve labeled " $P_1 + P_2 + P_3$ ") to exploit several paths simultaneously increases the on-time delivery probability to deliver the data within the deadline. In this specific example, path  $P_2$  becomes "useful" only for large deadlines, whereas  $P_3$  is "useful" for any deadline.

For multi-copy scheme, we consider only non-flooding algorithms, such that at most  $k$  copies of the packets are made throughout the execution (otherwise, an optimal flooding scheme can copy the data whenever there is a contact, namely in an *epidemic manner*, thus achieving the best possible delivery probability).

We propose a greedy Multi-Copy algorithm for on-time routing, denoted simply as MC-ONTIME. It computes the on-time delivery probability of all paths in isolation and choose the  $k$  best paths (without considering the interaction between them). This can be easily implemented by saving the best  $k$  paths while enumerating all possible paths as in ON-TIME. Moreover, our pruning mechanism is changed accordingly to consider the  $k$ -th best value discovered so far (rather the maximum value as in the single-copy settings)<sup>5</sup>.

However, since our algorithm works in a greedy manner, it does not consider the interaction between the paths, and more specifically the gain in probability over previously-selected paths (which can be very small in case the paths overlaps). This leads to a theoretical performance degradation with respect to an optimal, infeasible algorithm that considers the joint-probability over all sets of paths. The following theorem, whose proof is in Appendix F, provides tight bounds on this performance degradation:

**Theorem 1.** *The MC-ONTIME algorithm always achieves at least  $1/k$  of the on-time delivery probability of an optimal  $k$  multi-copy algorithm. In addition, there is a valid transportation graph for which MC-ONTIME achieves at most  $\frac{1}{(1-\varepsilon)^k}$  of the on-time delivery probability of an optimal  $k$  multi-copy algorithm, for arbitrarily small  $\varepsilon > 0$ .*

The performance degradation is mainly due to path overlapping; consider two paths with high success probability that differ only in one edge: MC-ONTIME will choose both paths, while, in fact, the marginal gain in choosing the second path is small. Thus, we consider also an algorithm that ensures that the paths are disjoint. Namely, the MC-ONTIME-DISJOINT algorithm iteratively chooses the path with the highest on-time delivery probability, among all paths from source to destination whose corresponding lines are not used by any previously-selected path. However, we show that the worst-case performance of MC-ONTIME-DISJOINT is the same as MC-ONTIME.

<sup>5</sup>When comparing to the heuristics of Sec. 4.3, we can similarly get the  $k$  paths with minimal expected traversal time, total headway or maximal success probability.

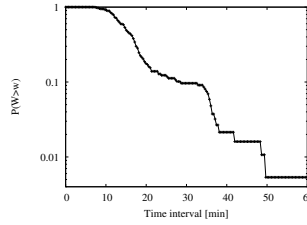


Figure 6: Complementary CDF of the critical time window  $W$  guaranteeing on-time delivery probability  $\in [0.1, 0.9]$  for the minimum expected traversal-time path.

Our simulations clearly show that the MC-ONTIME is superior in practice, and therefore this is the multi-copy routing algorithm we consider in the sequel.<sup>6</sup>

## 5 Performance Evaluation

We consider a set of 180 source-destination ( $s_s - s_d$ ) stop pairs; in the first 90 pairs both the source and the destination have been chosen uniformly at random in the entire metropolitan area; in the second 90 pairs, the source  $s_s$  is located in a main transportation hub within the city center (close to the main train station), and all the destinations  $s_d$  are chosen uniformly at random. We generate a set of 100 traces with the parameters obtained by the statistical analysis, covering all 250 lines for the four hours available from the schedule. In addition, we have developed a simulator that computes the delivery probability of each path by averaging across these 100 traces; note that the one day real-life trace alone would not be enough to compute this probability with any accuracy. Data is assumed to be available at the source stop at 7 AM.

For these 180  $s_s - s_d$  pairs, we start to evaluate the size of the “critical” time window defined as  $W = \phi(90) - \phi(10)$ : this is the amplitude of the interval of “reasonable” deadlines for which MIN-DELAY and ON-TIME(50) achieve delivery probability in  $[0.1, 0.9]$ ; intuitively, when considering any deadline outside this critical time window, one is either likely to fail or to succeed, and the randomness in the transportation system does not play a major factor. Fig. 6 shows the inverse CDF of  $W$ , considering the whole set of 180 pairs. For more than 90% of  $s_s - s_d$  pairs, the windows is larger than ten minutes and for more than 17% of them, it is even larger than 20 minutes. The maximum critical window size we observed is 67 minutes. As a consequence, the time window for which the deadline plays an important role on the delivery probability cannot be neglected for most of these 180  $s_s - s_d$  pairs.

Then, for all 180 pairs and for all 100 traces, we evaluate the optimal paths found by the ON-TIME algorithm and compare their theoretical on-time delivery probability with the empirical one determined by simulations. We found a reasonable agreement, even if not perfect in absolute values since in our model we assumed that line frequency and headway distribution do not change over time or between station along the same line; in real-life, there are small fluctuations in these values. In addition, while generating the synthetic traces, we introduce some inhomogeneity in the travel time

<sup>6</sup> MC-ONTIME-DISJOINT and MC-ONTIME are two extremes as for the amount of overlapping between the paths. In our future research, we plan to look also on hybrid heuristics with strict bounds on the number of overlapping edges. While these variants yield the same  $\frac{1}{k}$  worst-case approximation, they might be proved superior in real-life traces.

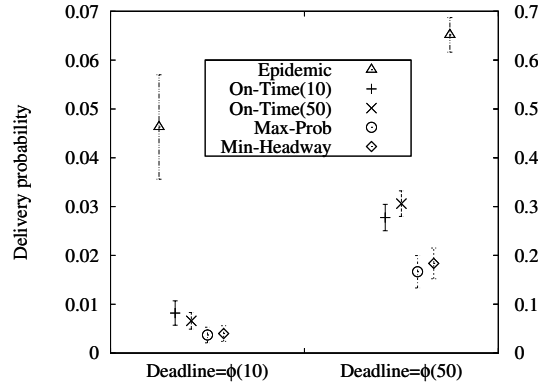


Figure 7: Delivery probability (average and 90% confidence interval) for two deadlines and different routing algorithms, for reliable transmission ( $p_f = 0$ ). MIN-DELAY is the same as ON-TIME(50).

distribution to ensure that buses maintain their order; our model, on the other hand, considers homogeneous travel time distribution that depends only on the scheduled travel time (See Appendix C).

We start to compare the performance of the algorithms defined in Sec. 4—namely, MIN-DELAY, ON-TIME, MAX-PROB and MIN-HEADWAY—with the EPIDEMIC algorithm that floods the network by taking advantage of all the possible contacts (and therefore making very large number of copies). We first assume that transmissions are reliable, i.e.  $p_f = 0$ . We evaluate the actual on-time delivery probability of the best path obtained by each algorithm; for each pair  $s_s - s_d$ , we set the deadline to  $\phi(x)$  for different values of  $x$ , and we compute the 90% confidence interval of the delivery probability considering all the possible 180 pairs. Due to the lack of space, we will report the results only for  $x = 10$  (“short deadline”) and  $x = 50$  (“average deadline”), since these cases are representative.

Fig. 7 compares the delivery probability of the different algorithms for the two deadlines. The gain on the delivery probability of EPIDEMIC with respect to all the other single-copy algorithms decreases as the deadline increases: the factor of gain is more than 5 for deadline  $\phi(10)$  and around 2-3 for deadline  $\phi(50)$ . Indeed, when the deadline is large enough, outside the critical time window, just one copy of the data is enough, independently from the actual path found by the specific routing algorithm; in such a case, EPIDEMIC does not introduce any gain in terms of performance, and the cost in terms of copies and transmissions is prohibitive (we observed on average more than 600 copies for  $\phi(10)$  and more than 900 copies for  $\phi(50)$ ) than the single-copy algorithms, for which the number of transmissions for each data is on average 5.5, and always less than 12.

ON-TIME(10) and ON-TIME(50) obtain the maximum delivery probability respectively, for deadline  $\phi(10)$  and  $\phi(50)$ , as expected. But comparing the corresponding confidence intervals, they behave almost the same. A somewhat surprising results is that in many cases (121 out of 180) ON-TIME(10) performs *exactly* as ON-TIME(50) (or, equivalently, as MIN-DELAY). In such cases, we verified by direct inspection that ON-TIME(10) and ON-TIME(50) select exactly the same optimal path.

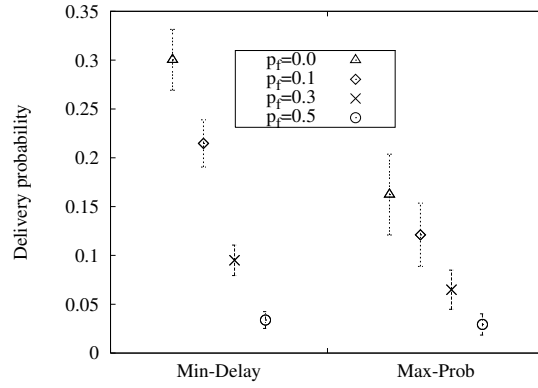


Figure 8: Delivery probability (average and 90% confidence interval) for MIN-DELAY (i.e., ON-TIME(50)) and MAX-PROB for deadline  $\phi(50)$  and for different values of transmission failure probability  $p_f$ .

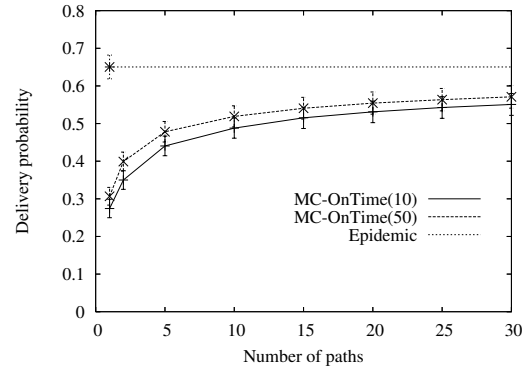


Figure 9: Delivery probability (average and 90% confidence interval) vs. number of paths for deadline  $\phi(50)$  and for multi-copy routing and no transmission failures ( $p_f = 0$ ).

These results have been confirmed also for other deadlines: ON-TIME(50) usually selects the best path computed by ON-TIME( $x$ ) for the deadline  $\phi(x)$ . Recall the example in Fig. 5, showing that the best path may depend on the deadline. While it is possible in a general setting, our experiments lead us to conclude that these cases are very rare in a real transportation system. Thus, one can choose the path solely on the basis of the minimum expected travel time (that is, the simple MIN-DELAY algorithm), making it redundant to run the complex optimal algorithm ON-TIME.

We now investigate the effect of transmission failures. Fig. 8 shows the delivery probability for different values of transmission failure probability  $p_f$ . When  $p_f$  increases, MIN-DELAY behaves very similarly to MAX-PROB; we expect that MAX-PROB becomes very efficient when the transmission failures are high, since the best policy must minimize the number of transmissions. Hence, both MIN-DELAY and MAX-PROB appear to behave very efficiently for large  $p_f$ .

We turn now to deal with multi-copy settings. Fig. 9 shows the performance of the MC-ONTIME policy, applied to the first best pre-computed paths found by each routing algorithm in all the considered 180 source-destination pairs, assuming reliable transmissions ( $p_f=0$ ). For deadline  $\phi(50)$ , ON-TIME with one copy reaches a delivery probability which is slightly less than half (more precisely, 42% and 47%) than the epidemic case, and few copies of MC-ONTIME improve the performance significantly by a factor 1.7-1.9. Yet, after 10 copies we observe only a negligible improvement. This is partially due to the fact that MC-ONTIME exploits a given sequence of paths provided by the algorithms, whose internal “diversity” among the paths is limited. Furthermore, EPIDEMIC exploits low-probability paths that are efficient just for the specific trace instance considered in each simulation run; since the number of these low-probability paths can be very large, due to the redundant connectivity of the bus transportation system metropolitan area, there might be a high probability that at least one of them will be used to deliver to the destination. Note that the cost in terms of transmissions and copies for EPIDEMIC (on average, more than 900) is two order of magnitude larger than the multicopy approach using a pre-selected subset of 10 paths.

## 6 Conclusions

This paper lays the foundations for a framework to analyze bus-based networks, where communication is between the mobile buses and the stops along their trajectories. Through a statistical analysis of traces, taken from a real transportation system of a large urban area, we were able to obtain a succinct stochastic graph representation of the system, and to devise routing algorithms on this graph. In addition, we were able to develop a synthetic trace generator, which in turn allowed us to perform an extensive simulation study, verifying the performance of our proposed algorithms.

An important outcome of this study is that, although different from the optimal but computationally-intensive algorithm, the simple MIN-DELAY algorithm achieves excellent results in term of success probability for any reasonable deadline. In addition, we show that increasing the number of data copies beyond 10 does not provide any meaningful boost in performance.

As final comment, we note that our model can be extended to bus-bus communications by introducing some *virtual stops*, located in correspondence to possible physical contact points between two different lines. By appropriate choice of weights on the corresponding edges (e.g., no waiting time and high failure probability), one can capture the nature of this kind of communication as well. The main challenge, left for future research, is to locate the physical contact points and to bound their number so that the running times of the algorithms remain feasible.

## A Comparison of Bus-Bus vs Bus-Stop Communications

For the scenario under consideration, where a rather large set of buses roam around a city, the prior work has primarily focused on transfer of messages through opportunistic links that are formed when two buses come within the proximity of each other. Apart from the physical layer restrictions such as scattering, slow and fast fading, this approach may cause problems because of insufficient contact time. Burgess *et al.* show that the contact duration between two mobile nodes can be very short to prevent the transfer of all the messages the nodes maintain in their buffers [10].

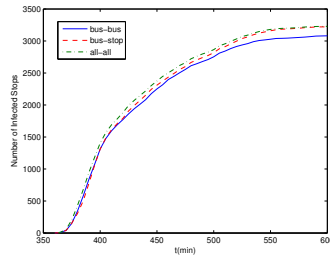


Figure 10: Comparison of Epidemic Routing with bus-bus & bus-stop communications

We now evaluate bus-bus and bus-stop communication paradigms without taking these effects into account. Instead, we look at how fast a message propagates in a transportation network using these two paradigms. Considering the schedule information for the buses as well as the location information of the stops, we have extracted the times when any two buses are supposed to form a link based on the schedule. Here, we used the common disc model where if the distance between two nodes are smaller than a threshold value at a given time, they are neighbors and one can transmit data to the other.

In Fig. 10, we compare the epidemic routing schemes with bus-bus and bus-stop communication approaches. In bus-bus approach, a bus can receive a packet only from another bus, i.e. only a bus can infect another bus. Stops are infected by buses but a stop can not infect the buses. In bus-stop approach on the other hand, the buses can only be infected by stops and vice versa. In all-all communications, all the contact opportunities (both bus-stop and bus-bus) are utilized. Here we assumed, a packet starts at a busy bus stop that serves many lines and epidemic routing proceeds without a particular destination stop. We evaluate how the number of infected stops increase over time. In bus-bus case, the source stop only infects the first encountered bus. The results show that bus-stop is at least as effective as bus-bus communications to spread the information. In fact, as the time progresses, the number of infected stops become identical with the all-all case whereas bus-bus communications may not diffuse the message to all the stops that bus-stop communications can.

Remember that this evaluation assumes perfect physical and link layers, and does not consider the effects of short contact duration, scattering, etc. In bus-stop communications, such effects are mitigated because the wireless links are formed between two stationary nodes as opposed to mobile nodes. The time in which passengers board and alight is much larger than the time two moving bus enter and exit each other's communication range.

## B Bus Mobility Models in Transportation

This investigation of the transportation literature is mainly based on the overviews in [12, 4].

Some works provide probability distribution for arrival time or lateness or delay, based on empirical studies (e.g. [43, 42, 19, 39, 40] or on model simplification (e.g., [1, 24]). Most studies prefer to use a skewed distribution since it is more likely to be behind schedule than ahead. Lognormal or gamma random variables are the most common assumptions (see the summary table in [12]).



About the statistical dependency of these quantities, contrasting effects hold. In general once a bus with low headway is late at a given stop, it is difficult to recover its lateness. In fact, for lines with low headways, passengers usually do not regulate their arrival on the basis of the schedule. Hence, passenger arrival can be assumed to be a Poisson process. When a bus is late, the longer waiting time at following stops causes an increase in the number of passengers who board (and later alight) resulting in longer dwell times and higher and higher delay en-route. Therefore, lateness and delay are positively correlated in such cases: high lateness at a stop results in increased delay over the subsequent segment [43]. This phenomenon does not always occur on buses with higher headway. In fact, passengers now tend to arrive just before the scheduled departure time of desired bus. Hence, late buses do not board significantly more passengers than on-time buses. Furthermore, since higher headway buses often have slack built into their schedule, there is opportunity to recover some of the lost time [23]. Penalties to drivers for being excessively late encourage them to catch up to the schedule. Thus, the delay in a segment is negatively correlated with the lateness at the start of the segment. Because of these two phenomena, the delay on a bus line segment can either be negatively or positively correlated with the lateness at the start of the segment, depending in large part on the line headway. Moreover, we observe that the lateness of a bus also has consequences on following buses on the same line and direction. A late bus boards more passengers, and so it leaves less of them for the following bus. This effect would lead to a negative correlation between the lateness of consecutive buses. At the same time in many cases transport agency policies or traffic conditions make overtaking impossible or quite rare. Hence a bus that is significantly late would cause also the consecutive ones to be late.

Regarding dwell time, this can be a significant part of the total service time (up to 16% of the total service time according to [4]). This time clearly depends on the number of passengers boarding and alighting (empirical formulas are proposed in [27] and [20]), but also on the crowding, fare types [19], payment modalities, bus design (separate/common doors for boarding and alighting), mode (i.e. bus or metro lines) and service type<sup>7</sup> [41]. Also, the contribution of dwell time to lateness correlation is not immediate. For example a large dwell time can be due to a large number of passengers boarding or alighting. In the first case the alighting at following stops will in general large, in the second will be small.

## C Generation of Tunable Synthetic Traces

In this section, we describe the evolution of building the synthetic traces, from the scheduled raw traces which we could have for a public bus transportation from the available schedules on their website.

Based on the empirical study and after performing a deep analysis on the *GTT* (*Gruppo Torinese Trasporti*) bus traces for a subset of bus lines, we could notice that lateness at following stops are highly correlated, where lateness at the initial stop, i.e.  $l(s_0)$  following the notion in Sec. 3, is triangularly distributed with support between  $[-2, +2]$  in minutes. On the other hand, it seems that the distribution of actual travel time is a lognormal, where the distribution parameters vary according to the scheduled travel time, *STT*. This observation complies with previous studies on the travel time in

<sup>7</sup> Service type can be rapid, limited, local, or combined depending on the vehicle speed, and the distance between consecutive stops.



transportation networks (See Appendix B). The following formulas are used to evaluate the mean and the variance of the travel time, denoted by  $M_{TT}$  and  $V_{TT}$ , respectively.

$$M_{TT} = 0.7(STT + 0.5) \quad (2)$$

$$V_{TT} = \frac{M_{TT}^2}{4} \quad (3)$$

The actual arrival time of a vehicle  $v$  at stop  $s_k$  is given in (1). The arrival time at  $s_0$ ,  $t(v, s_0)$  is the summation of the scheduled arrival time and the lateness at that stop,  $l(s_0)$ . While the arrival time at a following stop is the summation of actual arrival time at the previous stop and the actual travel time calculated based on the scheduled travel time, following the predefined lognormal distribution. Here the travel times and the lateness of the bus at the initial stop,  $l(s_0)$  are independently generated. The actual arrival time at stop  $s_k$  is given by:

$$t(v, s_k) = \begin{cases} \tau_k + l(s_k) & \text{for } k = 0 \\ t(v, s_{k-1}) + tt(v, s_{k-1}, k_i) & \text{for } i > 1 \end{cases}$$

Another observation from the real life traces is that the scheduled travel time for a vehicle between two consecutive stops is always less than 6 minutes. Although with low probability, the random variable generator can produce numbers that are greater than this value. In this case, we truncate the output of the generator to 6 minutes.

During the evolution of generating the synthetic traces and each time we calculate the actual arrival time, we should check if such actual travel time will cause a negative headway. In other words, one vehicle can overtake the previous vehicle on the same line, a phenomenon not observed in the real life traces. In this case, we generate another new independent travel time and re-evaluate the actual arrival time again while keep considering the negative headway effect. At the same time, we maintain these unused values in a queue. Before we generate a random value from a particular distribution, we check the queue if there is random variable in the queue generated from this distribution. If the value in the queue does not cause negative headway, it is used without generating a new random variable. At the end of each run, we see that there may be some values in the queue; however, their number is significantly less than the total number of values generated. Hence, we maintain the empirical distribution of the travel time.

## D Bus stations aggregation

In this section, we show how to aggregate the bus stations (stops) into groups. The goal behind aggregation is to reduce the number of attached wireless boxes at the stops. the stops physical location and the effective coverage range of the wireless boxes are the main parameters of the aggregation process. the coverage range is assumed to be homogeneous along all the stops. With a given coverage range find the stop that has the maximum number of neighbors in its range, this stop will be attached to a wireless box, the stop and its neighbor/s are considered to be in one group, we follow the same procedure to determine other group/s after neglecting the set of stops in the earlier found group/s.

Different transmission ranges are considered 50, 100, 150, 200 and 250 meters, table 1 shows the ratio of stops attached to the wireless boxes to the total number of

Table 1: Stops aggregation, in whole city

TX-RANGE	NO. GROUPS	NO. TOTAL STOPS	RATIO
50m	4385	6868	0.6385
100m	3464	6868	0.5044
150m	3055	6868	0.4448
200m	2752	6868	0.4007
250m	2394	6868	0.3486

Table 2: Stops aggregation, in downtown

TX-RANGE	NO. GROUPS	NO. DOWNTOWN STOPS	RATIO
50m	1552	2550	0.6086
100m	1084	2550	0.4251
150m	844	2550	0.3310
200m	687	2550	0.2694
250m	517	2550	0.2027

stops in the city. In our study we target to focus on the downtown, later in Appx. E we show how we could determine it, on basis of that it has no meaning to attach wireless boxes to stops located outside the defined downtown, thus we modify the aggregation to be applied only on stops physically located inside our interest area, table 2 shows the aggregation effect of the stops in the downtown.

## E Analysis of the Bus Graph

In this section, we overview the process of selecting the set of stops for our evaluation in Section 5. Even though the transportation network provides a decent coverage to the area, not all stops are connected to every other stop in the network through vehicles roaming in the city. To this end, we define the *bus graph* and analyze its properties such as connectivity. This analysis is performed on real life GPS traces of buses in Turin public transportation system. The traces are collected on a typical work day, from 6:00 am to 10:00 am.

The bus-graph is directed multi-graph where the vertices correspond to bus stops and are connected to each other based on the sequence of the stops each bus visits. A vertex is connected to another if a vehicle makes a stop at the first and consecutively at the second. Because there are potentially more than one bus that connects one vertex to another, multiple links are possible between them.

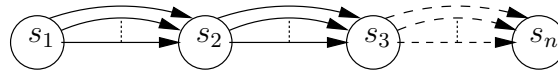


Figure 11: DTN Graph

It is also important to note that these links are not omni-present. Let  $B_{i,j}$  denote the set of buses/vehicles passing through stops  $s_i$  and  $s_j$ , consecutively. Each of these buses corresponds to an edge in the bus graph and is associated with a timestamp.  $T_{i,j}^m$ , the timestamp associated with vehicle  $m$  where  $m \in B_{i,j}$ , is a tuple  $(D_{i,j}^m, A_{i,j}^m)$ .  $D_{i,j}^m$  yields the time at which  $m$  departs from  $s_i$  for  $s_j$  and  $A_{i,j}^m$  if the arrival time at  $s_j$ . For end-to-end connectivity, the sequence of the links and their timestamps also matter. In

Fig. 11, there is a directed path from  $s_1$  to stop  $s_3$  if there is at least one path with  $A_{1,2}^x < D_{2,3}^y$  where  $x \in B_{1,2}$  and  $y \in B_{2,3}$ . Hence,  $s_1$  is connected to  $s_3$  over time.

From the bus graph, we obtain two new directed graphs  $G$  and  $G^t$ , where vertices are again bus stops. If one vertex is connected to another in the bus graph, there is a directed link from the first to the latter in  $G$ . In other words, in the graph deduced from the bus graph in Fig. 11, there is a link from  $s_1$  to  $s_3$  although they are never immediately connected. In order to form  $G^t$ , we look at the sequence of stops each bus follows without taking the associated timestamp into account. If there is at least one vehicle that travels from one stop to another stop, there is a directed link from the first to the second in  $G^t$ . Discarding the timestamps in  $G^t$  is motivated by the periodicity of buses that belong to the same line. In a bus network, a group of buses follow the same routes, i.e. a sequence of the stops. If one bus follows a particular sequence, it is like that another bus will repeat this sequence in the future.

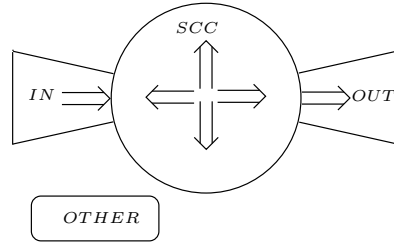


Figure 12: DTN Graph components

We start our evaluation by categorizing the vertices in  $G^t$  into four groups:

- The Strongly Connected Component (SCC) in which every node is connected to every other node. There is at least one directed edge from one stop to another; the reverse edge also exists.
- IN component in which there is a directed edge from every stop to SCC. Note that being connected to one stop in SCC also translates as being connected to every node in SCC. However, there is not a directed edge from a stop in SCC to a stop in IN.
- OUT component. There exists a directed edge from SCC to the every stop in this component but there is no reverse edge from a stop in OUT to SCC.
- OTHER component consisting of stops that are completely isolated from SCC.

These categories are depicted in Fig 12.

We have seen that the largest group in  $G^t$  is SCC that consists of 5182 stops, 96% of the whole. There are 151 stops on IN component. Looking at the schedule, we note that these stops serve to the special shuttles that only operate in the morning to pick up some employees and take them to their work places in the city center. Although these shuttles are also scheduled to run in opposite direction, the return trip takes place in the evening hours which is beyond the time we looking at the network. OUT component consists of 67 stops. These stops are similar to those in IN; however, these are associated with the shuttles that carry people who work in the suburbs. The return trips for these shuttles are also scheduled for the evening hours. The number of stops in OTHER component is 2. Fig. 13 shows the physical location of the stops and indicate what component they

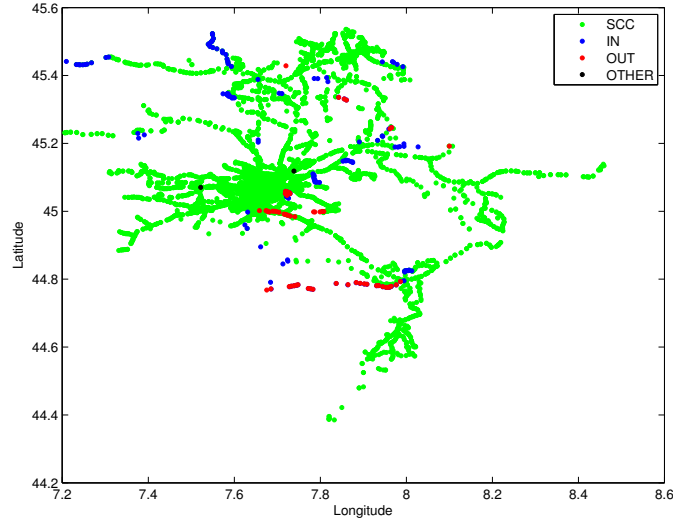


Figure 13: Bus graph components (SCC, IN, OUT and OTHER)

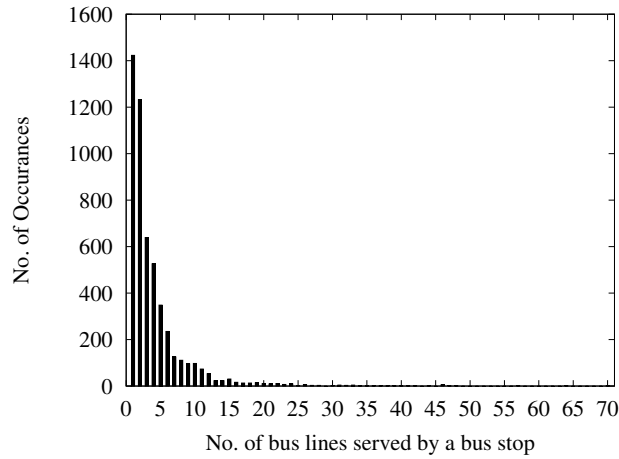


Figure 14: No of stops serving a given number of lines

belong to. Among these components, only SCC guarantees complete connectivity. Although there is an edge from a stop in IN to SCC and from there to OUT but there might not be a directed edge from one in IN to another one in the same component. The rest of the analysis on  $G^t$  is performed only on SCC.

We now look at the distribution of the bus lines to the stops. Each line usually serves on multiple directions. In Fig. 14, we show the distribution of the directed bus lines a bus stop can serve. Our analysis shows that a bus stop serves at least one directed line while the maximum number of directed lines it can serve is 70. The stops in the city center are more likely to serve more lines. The figure also shows that a large number of stops serve a small number of bus lines. This property can be used to reduce the cost of wireless box implementation. Instead of installing a wireless box to each stop, we

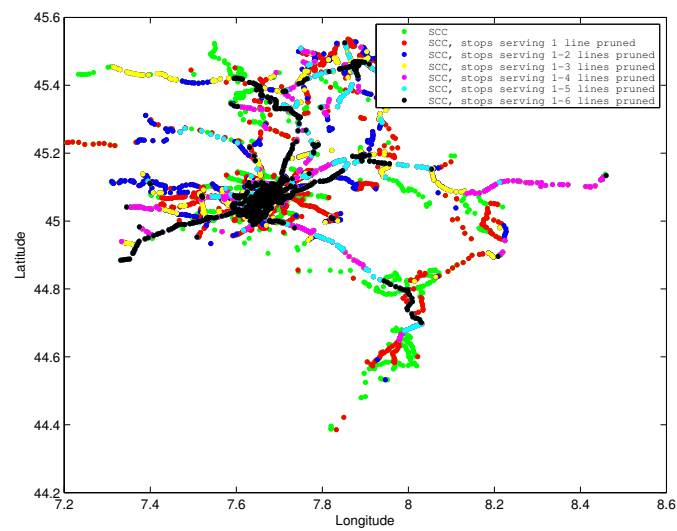


Figure 15: Bus stops map

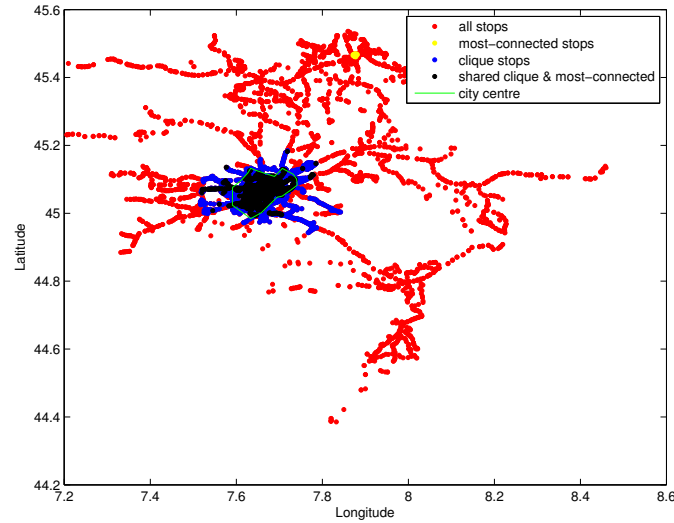


Figure 16: Identifying the city center.

can omit some stops since the number of transfer opportunities at these stops is limited and it is possible to spread the messages to lines these stops serve at other locations. We achieve this pruning the stops within the SCC considering the number of lines they serve. Doing this, we make sure that the remaining part is still strongly connected. In other words, we try to obtain the maximal clique in SCC, which is an NP-Complete problem. We follow a simple heuristic in which all the stops that serve up to seven lines are pruned. This way, the number of required wireless boxes decrease from 5402 to 874 while still maintaining the connectivity requirement. Fig. 15 shows the stops in the SCC with respect to the number of lines we consider when pruning the stops. Note that SCC with stops serving up to 2 directed lines pruned includes the entire SCC with stops serving up to 3 and more lines pruned. So, there are also overlapping stops in this figure.

Now, we move on to the connected part in  $G$ . We aim to find the maximal clique, i.e. the largest group in which every vertex is connected to every other vertex. The difference between the SCC of  $G^t$  and the maximal clique of  $G$  is that the maximal clique also considers the sequence of timestamps in path formation. Therefore, maximal clique is smaller in size than the SCC. Our findings show that only 2943 stops fall in the maximal clique (without pruning).

Since we consider the timestamps and not the periodicity of the buses, we evaluate the busyness of stops by the number of buses they serve instead of the lines. After ranking the stops according to the number of scheduled stop-bus meetings in the descending order, we take the set of buses that hosts the half of such meetings. This set is called the most connected stops. Depending on the maximal clique and the most connected stops, we determine the boundaries of the city center. Fig. 16 shows the location of the most connected stops and the stops in the maximal clique. The polygon that contains (almost) all the stops in the intersection of the maximal clique and the most connected stops yields the city center. We see that there is a good match between the Turin downtown area and the polygon in Fig. 16.

## F Tight Bounds on the Performance of Multi-copy Algorithms

In this section we provide the proof for Theorem 1 of Section 4.4, which deals with the performance of the multi-copy MC-ONTIME algorithm. This algorithm computes the success probability of all paths in isolation and chose the  $k$  best paths (without considering the interaction between them). Theorem 1 comprises of the following lower- and upper-bounds.

**Lemma 1.** *The MC-ONTIME heuristic always achieves at least  $1/k$  of the success probability of an optimal  $k$  multicopy heuristic.*

*Proof.* Let  $p_1, \dots, p_k$  be the success probability of the paths selected by the MC-ONTIME algorithm, such that  $p_i$  corresponds to the path selected at iteration  $i$ . Let  $q_1, \dots, q_k$  be the success probability of the paths selected by the optimal algorithm, and by  $Q_1, \dots, Q_k$  the corresponding events (namely,  $\Pr[Q_i] = q_i$ ). Note that by definition,  $p_1 \geq \max_i q_i$ .

Thus,

$$\Pr[\text{GREEDY succeeds}] \geq p_1 \geq \frac{1}{k} \sum_{i=1}^k q_i \geq \frac{1}{k} \bigvee_{i=1}^k Q_i = \frac{1}{k} \Pr[\text{The optimal algorithm succeeds}],$$

where the third inequality is due to the union bound.  $\square$

**Lemma 2.** *There is a valid transportation graph for which MC-ONTIME achieves at most  $\frac{1}{(1-\varepsilon)^k}$  of the success probability of an optimal  $k$  multicopy algorithm, for arbitrarily small  $\varepsilon > 0$ .*

*Proof.* Consider a transportation graph in which, from the source to the destination, there  $2k$  paths as following:

- $k$  two-edge paths, which share their first edge. The probability to traverse this first edge is  $p$  while the probability to traverse the second edge is  $1 - \varepsilon/4$ .
- $k$  single-edge paths, such the probability to traverse the edge is  $p(1 - \varepsilon/2)$ .

Assume  $p = \frac{\varepsilon}{(k-1)(1-\frac{\varepsilon}{2})^2}$ .

The MC-ONTIME algorithm will choose the first  $k$  paths, since  $p(1 - \varepsilon/4) > p(1 - \varepsilon/2)$ . Since all these paths need to traverse the first edge, the probability that MC-ONTIME succeeds is at most  $p$ .

On the other hand, the optimal algorithm will do better than the algorithm that chooses the last  $k$  paths. The inclusion-exclusion principle (a.k.a Bonferroni inequality) yields that the success probability of the optimal algorithm is at least

$$kp(1 - \varepsilon/2) - \binom{k}{2} p^2 (1 - \varepsilon/2)^2$$

. This implies that the ratio between the success probability is at most

$$\frac{p}{kp(1 - \frac{\varepsilon}{2}) - \binom{k}{2} p^2 (1 - \frac{\varepsilon}{2})^2} = \frac{1}{k(1 - \varepsilon)}$$

.

$\square$

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INRIA - Domaine de Voluceau - Rocquencourt, BP 105 - 78153 Le Chesnay Cedex (France)  
<http://www.inria.fr>  
ISSN 0249-6399